

**Future Value of a Lump Sum Investment**

$$\text{Future Value} = \text{Principal} * (1 + \text{Rate})^{\text{Time}}$$

**Future Value of a Series of Investments**

$$\text{Future Value} = \text{Deposit} * \frac{(1 + \text{Rate})^{\text{Time}} - 1}{\text{Rate}}$$

1) Your grandaunt, Isabelle Ringing, just recently passed away and left you, her favorite grand-neice/grand-nephew, \$10,000. She always told you how important it was to save money for a rainy day. Resisting the urge to blow the entire amount on durable and non-durable consumer items, you put the money into an investment that earns 10% over 10 years. How much will you have at the end of 10 years? Is this enough for a car or a down payment on a house?

**\$10000**  
10%  
10 years

Single investment  
lump sum investment  
lump sum principal  
"Top Table"

10%  
10 years  
"future value multiplier" **2.594**

**\$10000** single investment  
**\* 2.594**  
**\$25,940** after 10 years

2) Ben Dover is thirty years old. This year, he plans to start putting \$5,000 per year into a Roth IRA (What's a Roth IRA? It's a retirement account.) and will continue to do so until age sixty, a total of 30 years. At 10% annually, how much will Ben have in his Roth IRA?

**\$5000** per year  
10%  
30 years

Series of deposits  
stream of investments  
stream of payments  
"Bottom table"

10%  
30 years  
"future value multiplier" **164,494**

**\$5000** per year  
**\* 164.494**  
**\$822,470** after 30 years

How much did he invest over 30 years?  
**\$5000** per year  
**\* 30 years**  
**\$150,000** invested

3) Eileen Forward, Ben's cousin, is 20 years old. She puts \$5,000 into a Roth IRA until age 30, only 10 years and then stops making contributions. With the same 10% annual rate, how much will Eileen have at age 60? (Hint: You'll need both future value tables.) Since Ben is saving \$5,000 for 30 years while Eileen is only saving \$5,000 for 10 years, Ben is sure that he'll have much more money than Eileen. Is he right?

**\$5000** per year  
10%  
10 years, then stop and hold for 30 years

① age 20  
age 30

Series of deposits  
**\$5000** per year  
10% - 10 years  
**\* 15.937**  
**\$79,685** after 10 years

② holds for 30 years  
lump sum principal  
**\$79,685**  
10% - 30 years  
**\* 17.449**  
**\$1,390,423.50**

How much did she invest?  
**\$5000** per year  
**\* 10 years**  
**\$50,000** invested

4) Neil Downe, their friend, is 18 years old. He is already a Fourbucks, uh, Fivebucks, sorry, Starbucks addict. He stops by there at least once a day. Ben & Eileen are trying to get him to give up his habit and place the money into a Roth IRA. If he puts just \$2 per day, \$60 per month, into the same Roth IRA, how much will he have at age 68? What if he saves \$5 per day, \$150 per month?

**\$5** per day  
**\$150** per month  
**\$1800** per year  
10% - 50 years

series of deposits  
**\$1800** per year  
10% - 50 years

**\$1800**  
**\* 1163.909**  
**\$2,095,036.20!**

How much did he invest?  
**\$1800** per year  
**15 years**  
**\$9000** invested

5) Now try some other compound rates of return. Recalculate the above problems for 5%, 8%, 12% and 13%.